

# Single top quark physics

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on behalf of the CDF and D0  
collaborations

Les Rencontres de  
Physique de la Vallée  
d'Aoste

Wednesday,  
February 27, 2008

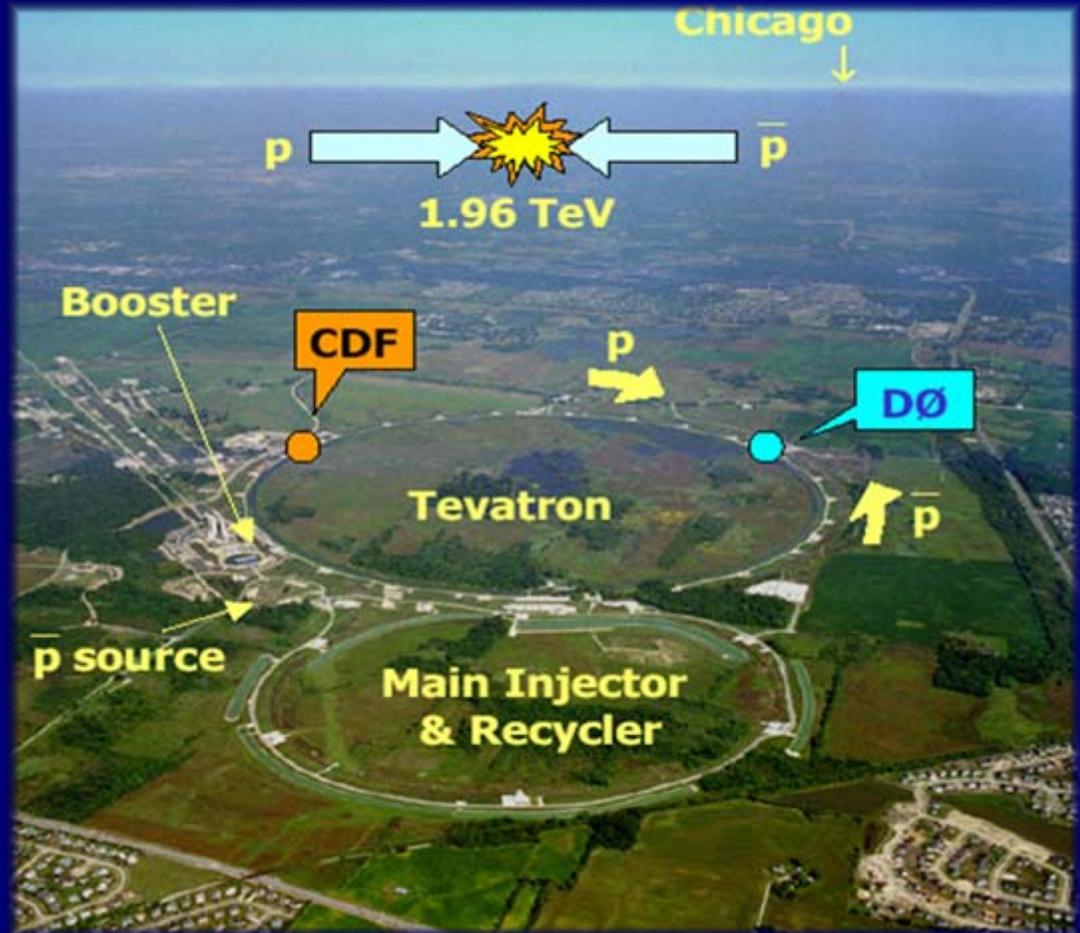


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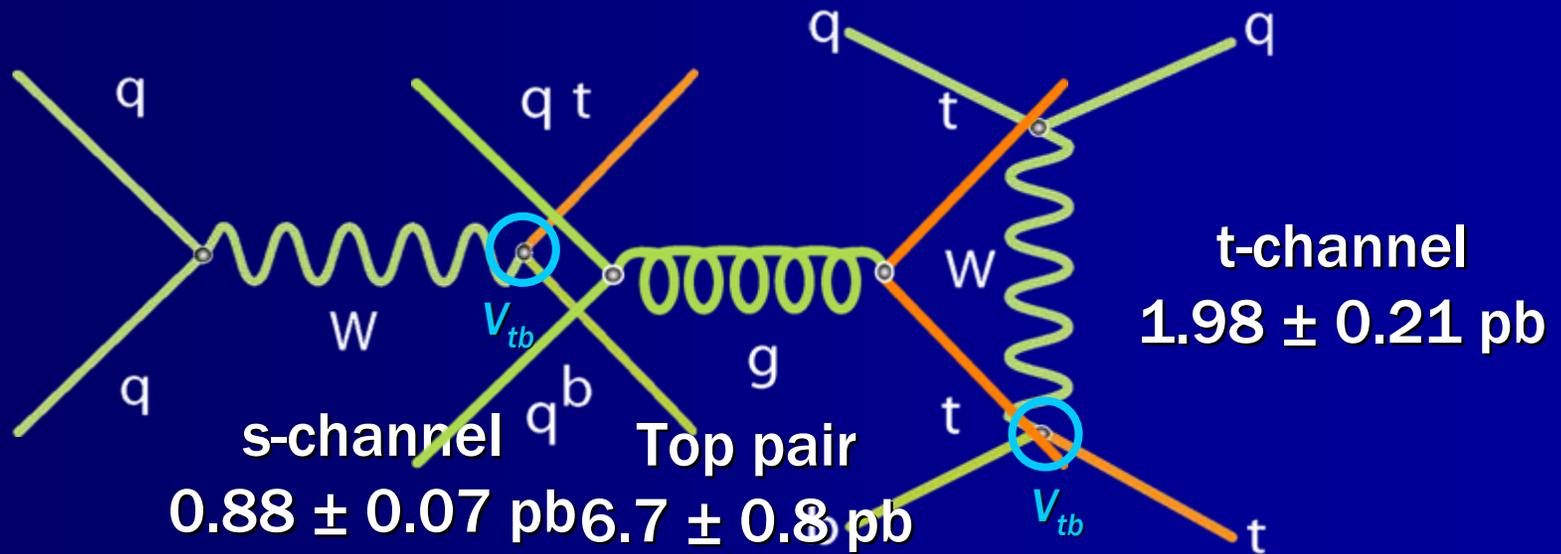


# The Tevatron

- World's highest-energy operational particle accelerator
- Two multi-purpose particle detectors, CDF and DØ
- The only place in the world to study top quarks (for now)



# Electroweak single top production

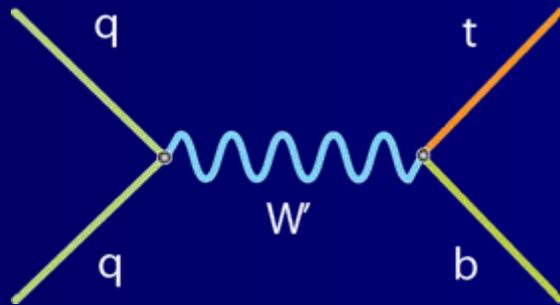
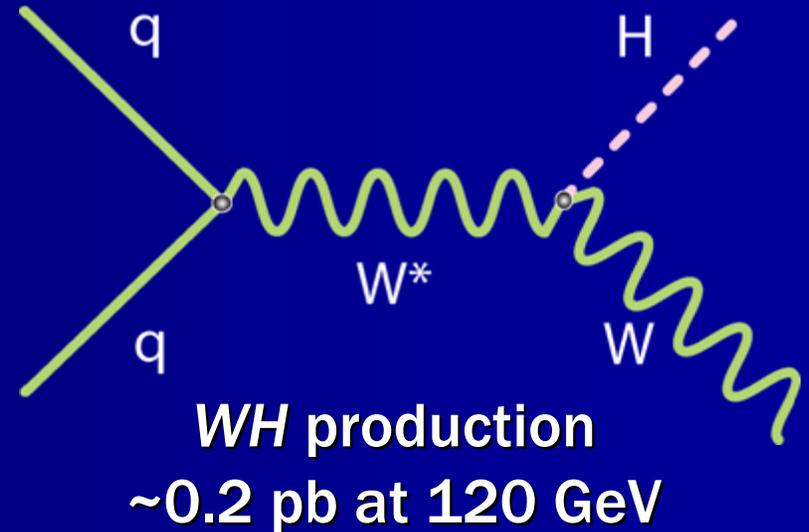


- Electroweak single top production allows in pairs by the strength of CKM matrix element  $|V_{tb}|$** 
  - Chance to measure polarized top quarks,  $W$  helicity**

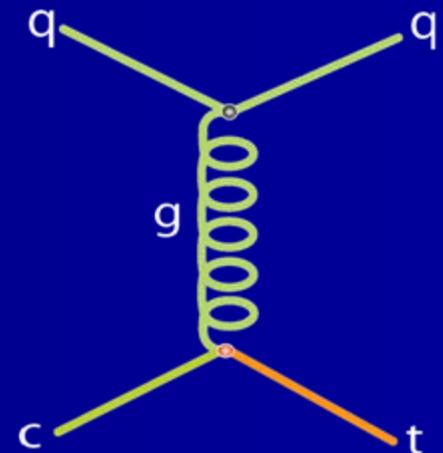
Quoted cross-sections at  $M_{\text{top}}=175 \text{ GeV}/c^2$  — Cacciari et al. JHEP 0404:068; Z. Sullivan, hep-ph/0408049

# Sensitivity to new physics

- Single top has similar experimental challenges to  $WH$ 
  - $WH$  is preferred channel for low-mass Higgs production at the Tevatron
  - Have to find single top to find Higgs in this channel!

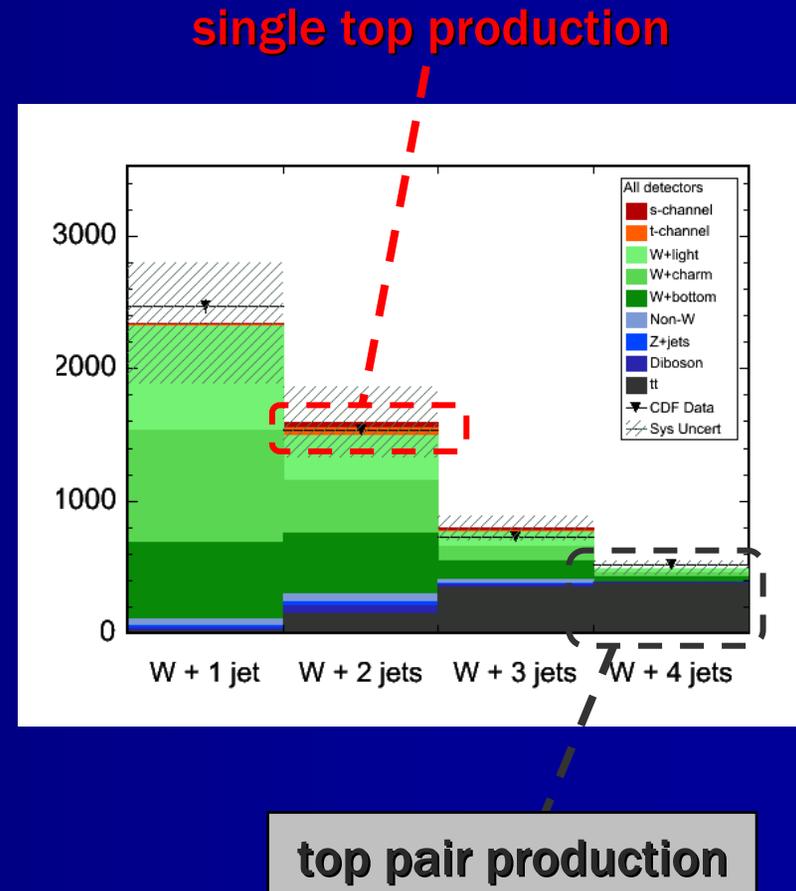


Also sensitive to heavy  $W'$ , flavor-changing neutral currents, Kaluza-Klein heavy  $W^{kk}$ , ...



# Experimental challenge

- Top quark pairs produce a final state with a lepton, missing transverse energy, and four jets — a distinct signature
  - Signal : background of about 3.4 : 1
- Single top production, with a smaller cross section and two fewer jets, is much harder to find
  - Signal : background of about 1 : 15
  - A simple counting experiment is impossible!



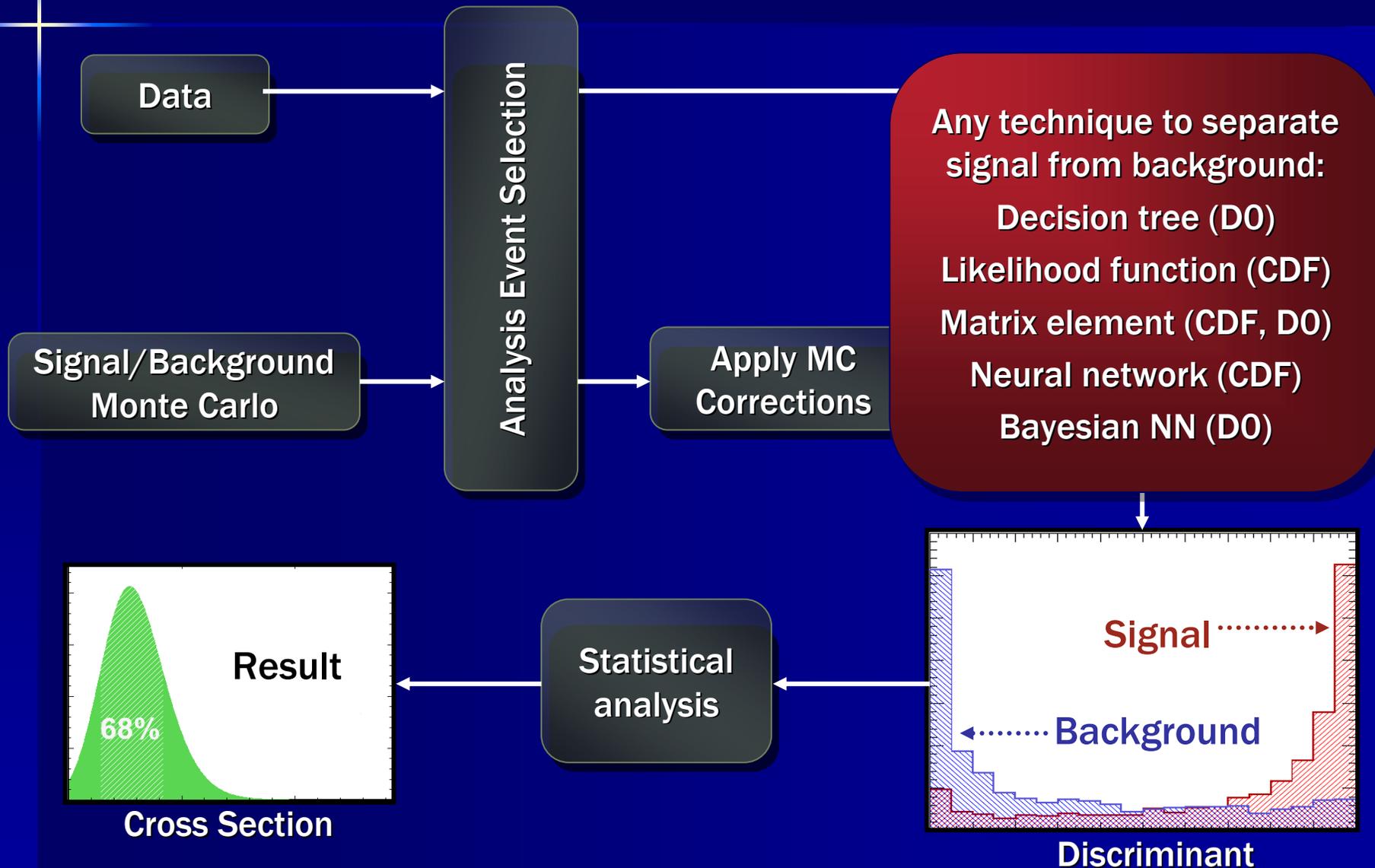


Although searching for something so tiny may seem hopeless...

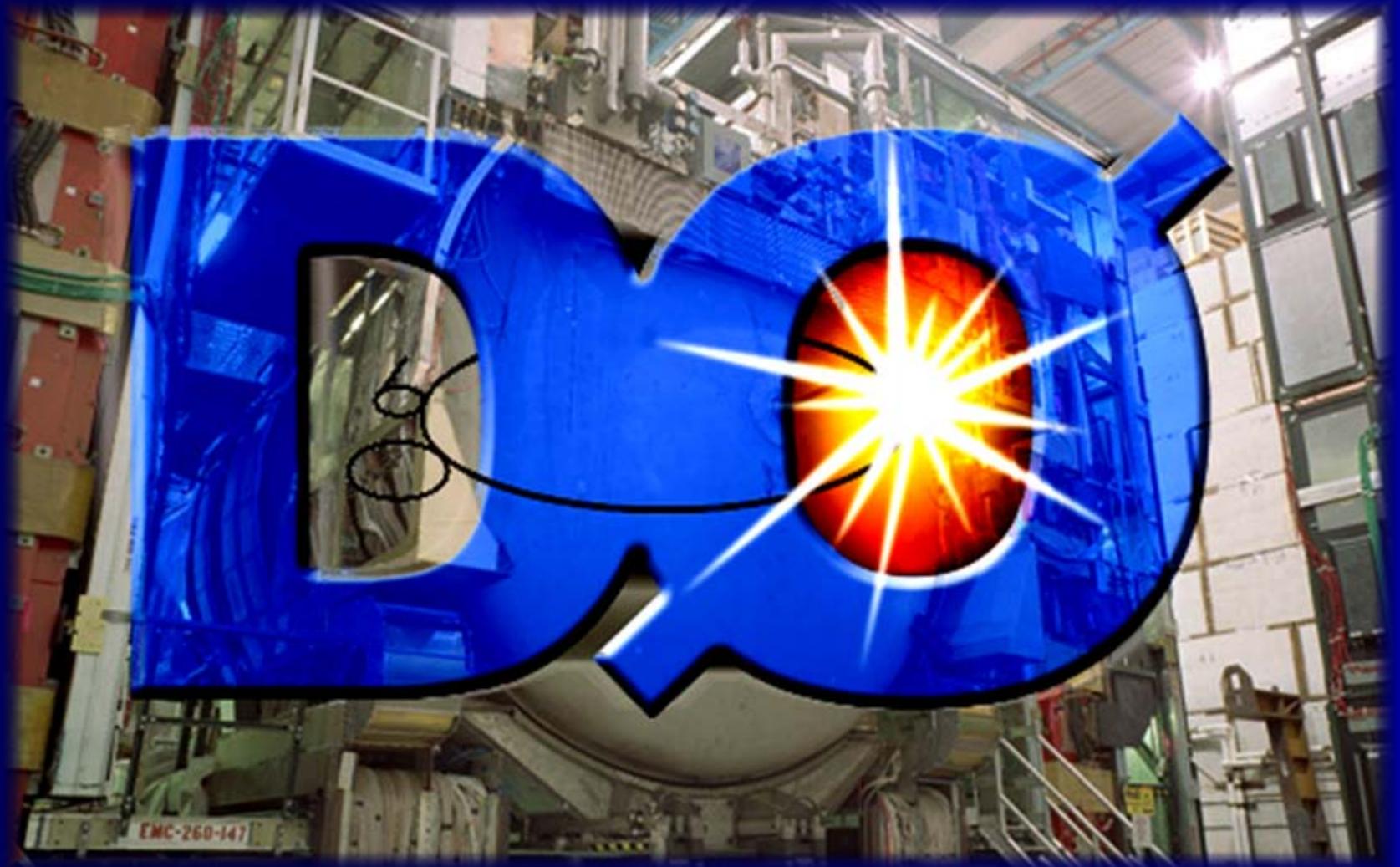


...We are still sensitive to the effects if we know what to look for

# General analysis method



# D0 single top search in $910 \text{ pb}^{-1}$



# Event selection and background estimate

Percentage of single top  $tb+tb$  selected events and S:B ratio (white squares = no plans to analyze)

Electron + Muon	1 jet	2 jets	3 jets	4 jets	$\geq 5$ jets
0 tags	10% 1 : 3,200	25% 1 : 390	12% 1 : 300	3% 1 : 270	1% 1 : 270
1 tag	6% 1 : 100	21% 1 : 20	11% 1 : 25	3% 1 : 33	1% 1 : 53
2 tags		3% 1 : 11	2% 1 : 15	1% 1 : 38	0% 1 : 43

Events in  $0.9 \text{ fb}^{-1}$  Data

1 tag+2 tags	3 jets	4 jets
$8 \pm 2$	$2 \pm 1$	
$2 \pm 3$	$4 \pm 1$	
$32 \pm 7$	$11 \pm 3$	
$103 \pm 21$	$143 \pm 33$	
$20 \pm 24$	$35 \pm 7$	
$35 \pm 17$	$23 \pm 5$	
$43 \pm 9$	$12 \pm 2$	
$77 \pm 15$	$29 \pm 6$	
$60 \pm 59$	$253 \pm 38$	
455	246	

$V_e$

W

t

$\bar{q}$

# Matrix element method

- Calculate probability density of an event resulting from a given process

Integrate over parton-level quantities

Parton distribution functions

$$P(p_1^\mu, p_{j1}^\mu, p_{j2}^\mu) = \frac{1}{\sigma} \int d\rho_{j1} d\rho_{j2} dp_v^z \sum_{comb} \phi_4 |M(p_i^\mu)|^2 \frac{f(q_1)f(q_2)}{|q_1||q_2|} W_{jet}(E_{jet}, E_{part})$$

Inputs:

lepton and jet 4-vectors – no other information needed!

Matrix element:

Different for each process.  
Leading order, obtained from MadGraph

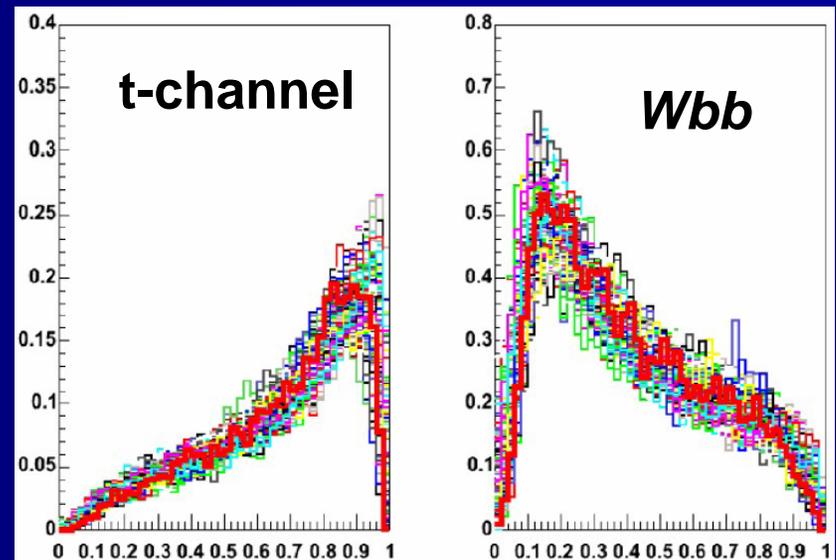
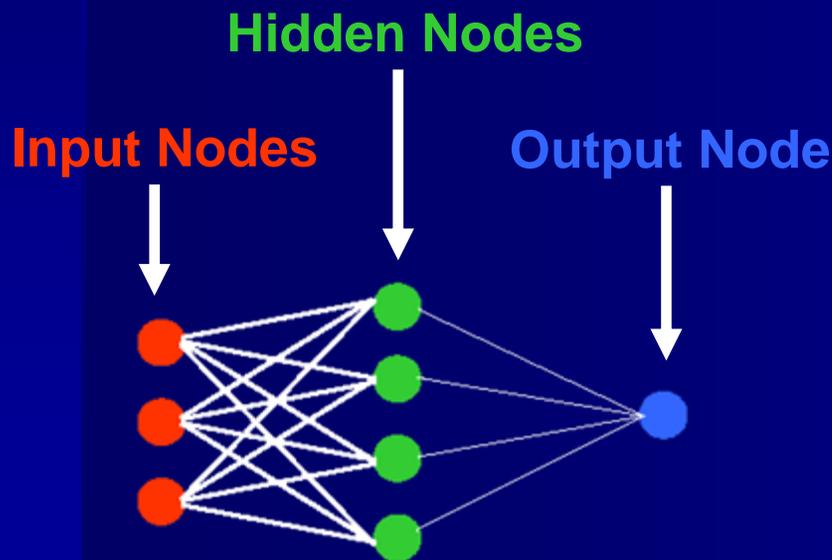
Transfer functions:

Account for detector effects in measurement of jet energy

- Uses full kinematic information of an event to discriminate signal events from background events
- Calculate probabilities for s- and t-channel,  $W_{bb}$ ,  $W_{cj}$ ,  $W_{gg}$ , and  $t\bar{t}$ -bar (for three-jet events)
- Use matrix element probability densities to create a discriminant: signal / (signal + background)

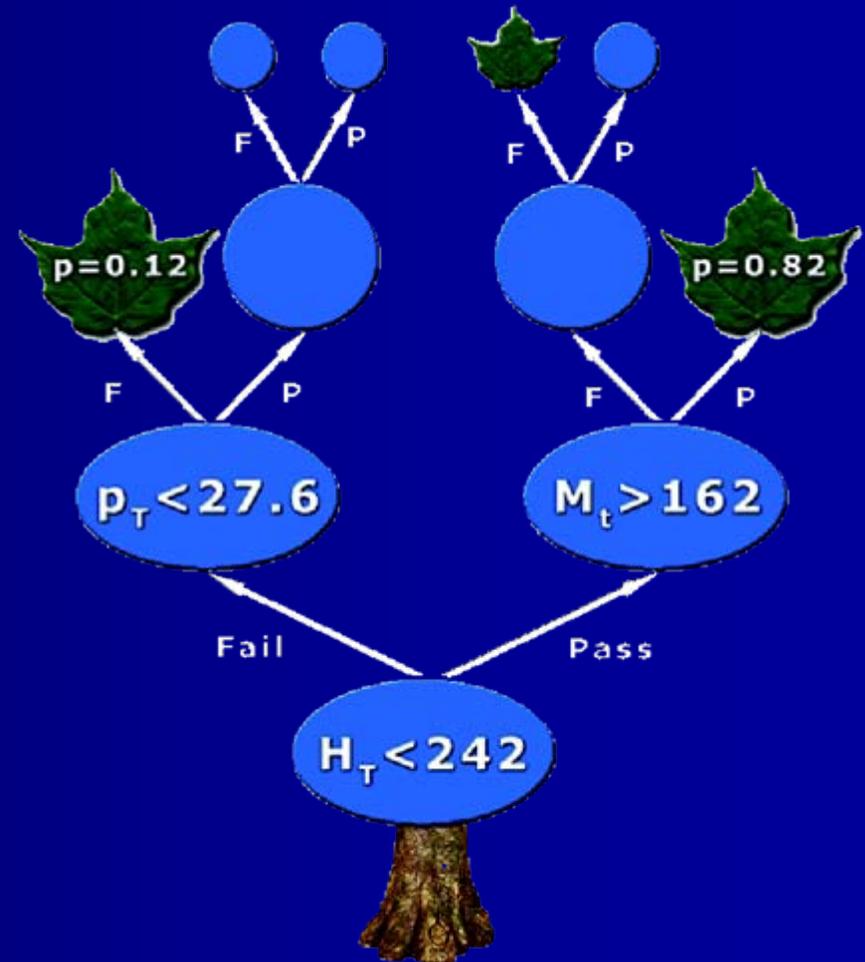
# Bayesian neural network

- Neural networks are trained on Monte Carlo to discriminate signal from background
- A Bayesian neural network is a weighted average of many networks
- Protected against overtraining



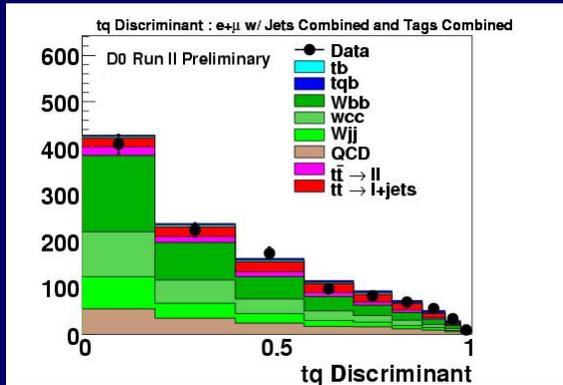
# Boosted decision tree

- Start with large number of input variables (49)
- Optimize series of binary cuts in Monte Carlo
  - Automatically finds “interesting” variables
- Sort events by output purity
- Create series of “boosted” trees by reweighting based on misclassified events



# D0 results

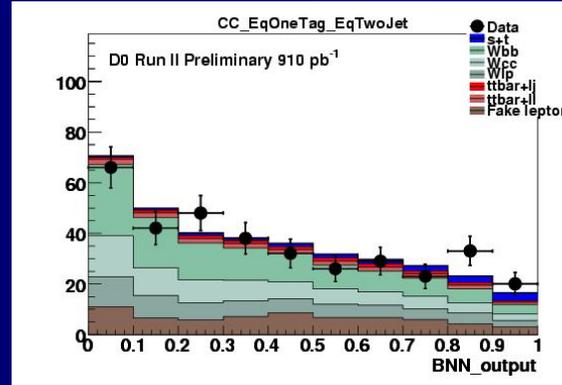
## Matrix element method



Measured cross section:

$$4.8^{+1.6}_{-1.4} \text{ pb}$$

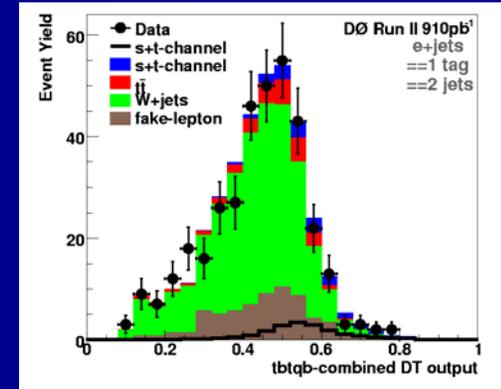
## Bayesian neural network



Measured cross section:

$$4.4^{+1.6}_{-1.4} \text{ pb}$$

## Boosted decision tree

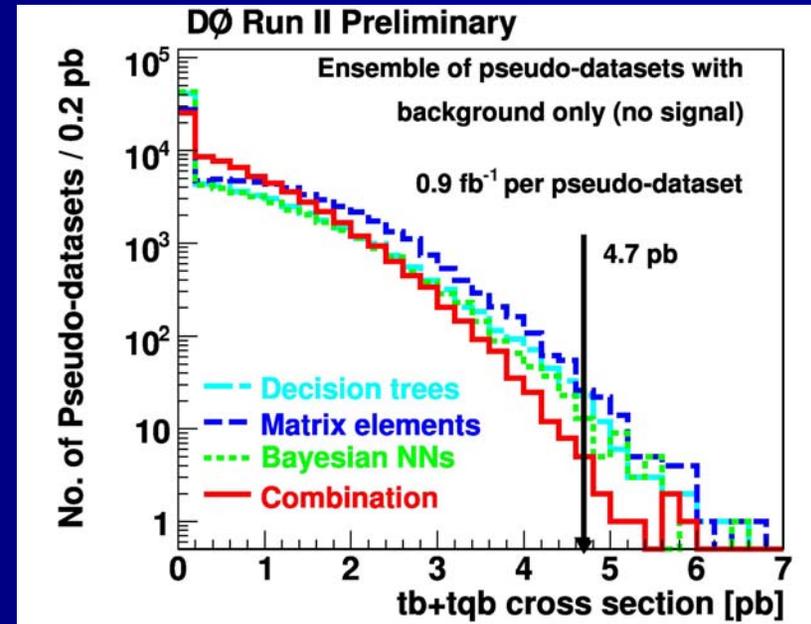


Measured cross section:

$$4.9^{+1.4}_{-1.4} \text{ pb}$$

# D0 combination

- Results are not fully correlated — can gain sensitivity by combining
- Combine results with best linear unbiased estimator (BLUE) method



Measured cross section:

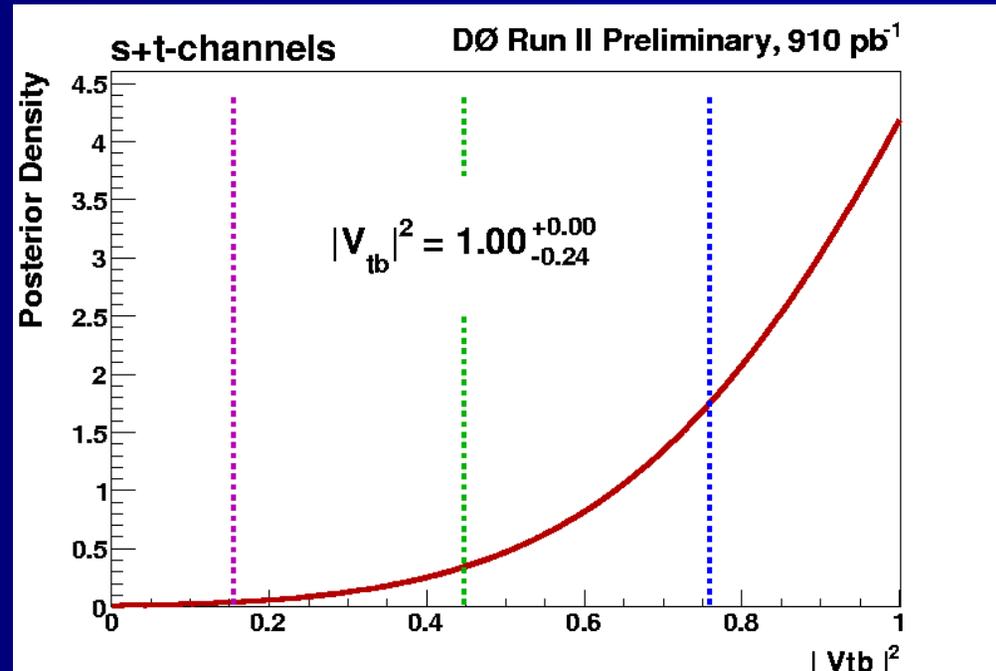
**$4.7 \pm 1.3$  pb**

Expected sensitivity:  
**0.011 (2.3 $\sigma$ )**

Observed p-value:  
**0.00014 (3.6 $\sigma$ )**

# DØ $|V_{tb}|$ measurement

- Derive a limit on  $|V_{tb}|$  based on boosted decision tree result
- Assume that  $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$



$|V_{tb}| > 0.68$  at 95% C.L.

# CDF single top search

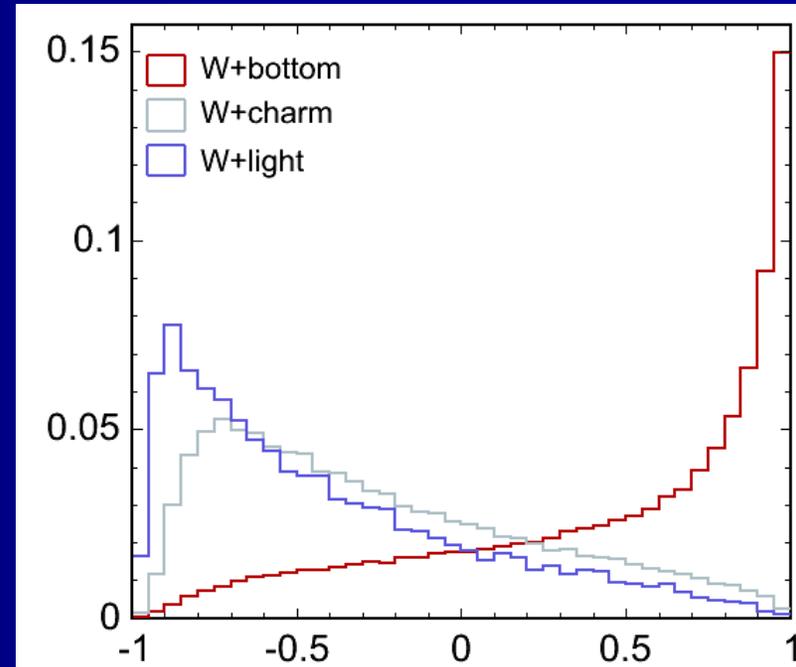


# CDF search in $1.5 \text{ fb}^{-1}$

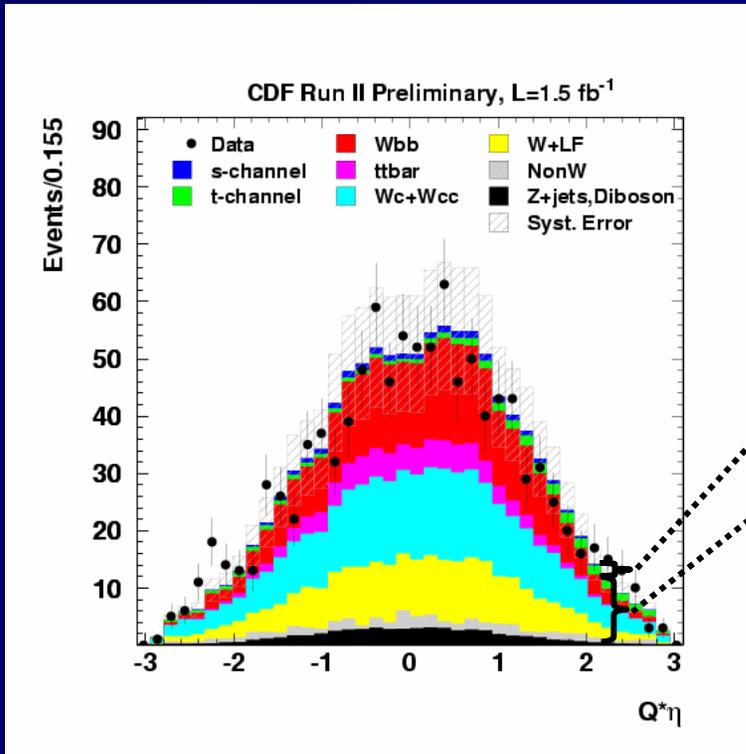
- In summer 2007, CDF also reported evidence for single top production with a two analysis methods: a matrix element method and a multivariate likelihood function
- D0 and CDF use similar approaches for the matrix element
- Expected sensitivity of  $3.0\sigma$ ; observed significance of  $3.1\sigma$

# Jet flavor separator

- CDF analyses use a neural net to separate jets from  $b$ -quarks from light-quark jets
- Produces a continuous output – not a cut
- Improves sensitivity by 10–20%!



# Multivariate likelihood function



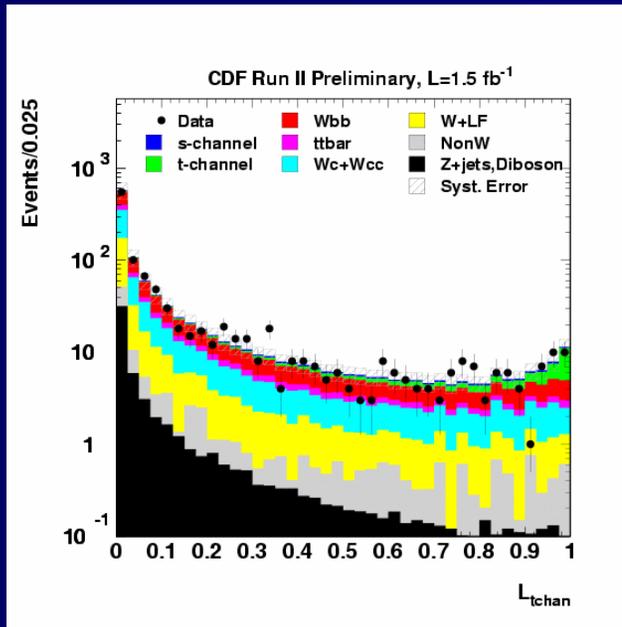
- Multivariate binned likelihood combines several sensitive variables into a single discriminant
- Pioneered at LEP
- Seven variables in this analysis

$$\frac{N_i^{sig}}{N_i^{bkg}} \rightarrow p_i^{sig} = \frac{N_i^{sig}}{N_i^{sig} + N_i^{bkg}}$$

$$L(\vec{x}) = \frac{\prod_{i=1}^{n_{var}} p_i^{sig}(x_i)}{\prod_{i=1}^{n_{var}} p_i^{sig}(x_i) + \prod_{i=1}^{n_{var}} p_i^{bkg}(x_i)}$$

# CDF results with $1.5 \text{ fb}^{-1}$

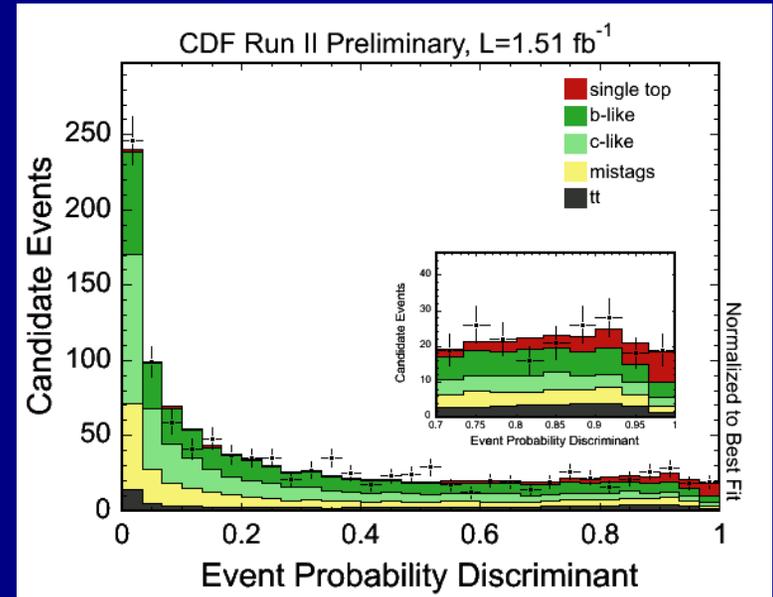
Likelihood function



Measured cross section:

$$2.7^{+1.3}_{-1.1} \text{ pb}$$

Matrix element



Measured cross section:

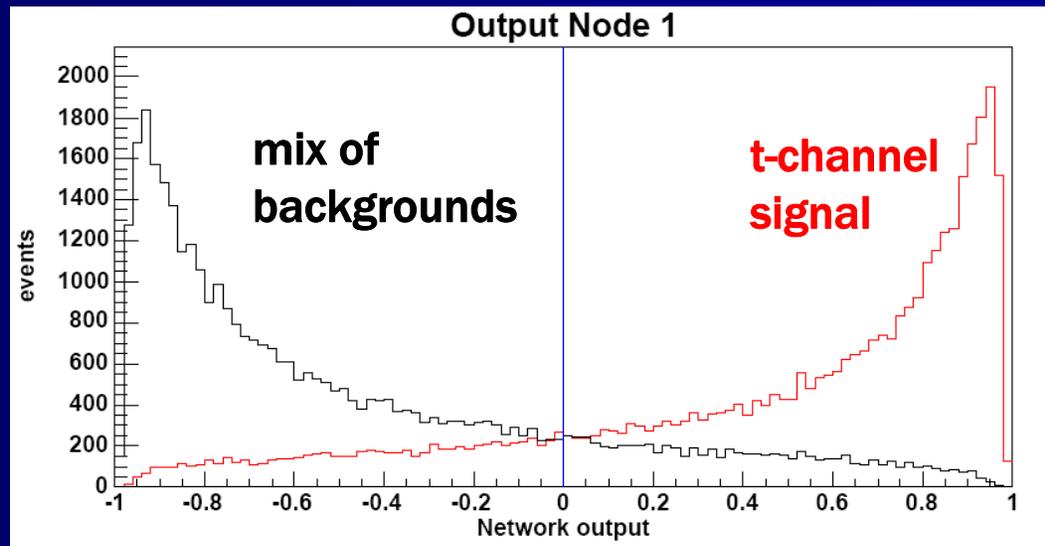
$$3.0^{+1.2}_{-1.1} \text{ pb}$$

# More improvements

- **Want to improve precision of measurement as much as possible**
  - Add more data (another 700 pb<sup>-1</sup>)
  - Update neural network analysis
  - Increase acceptance
  - Improve separation of signal and background
- **These will reduce expected uncertainty on the single top cross section, and thus  $|V_{tb}|$**

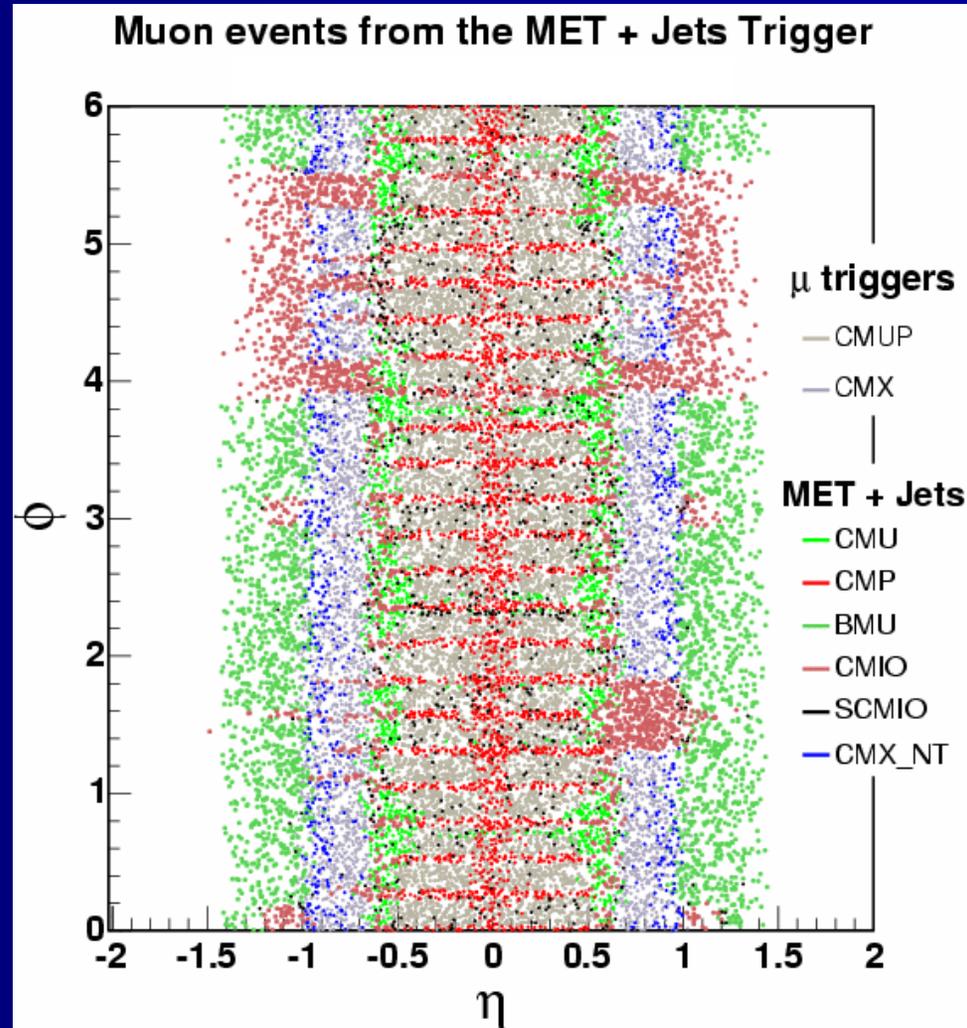
# Neural network

- Update neural network measurement last used for  $955 \text{ pb}^{-1}$
- Train separate networks for different tag multiplicities, based on the  $b$ -quark composition of each signal sample:
  - Train for t-channel for single-tagged events
  - Train for s-channel for double-tagged events



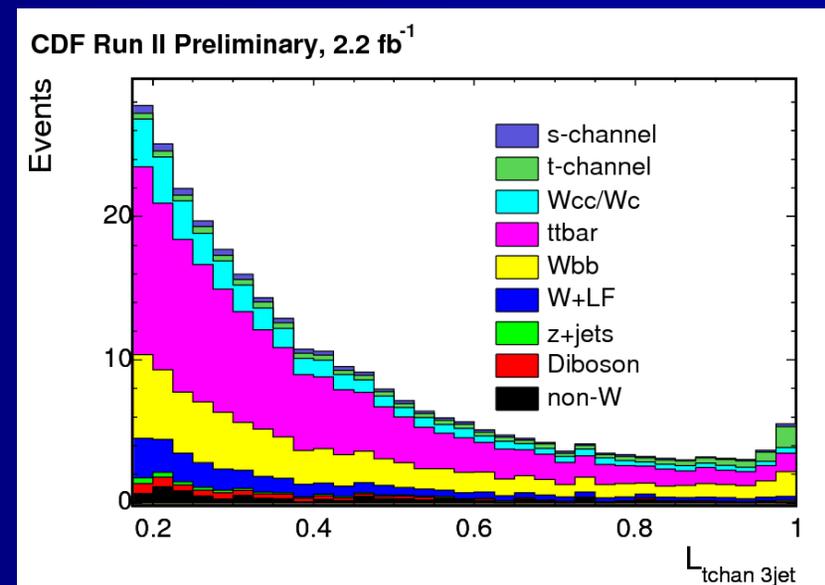
# Extended muon coverage

- Increase acceptance by taking muons from complementary trigger (missing  $E_T$  plus two jets)
- New muons “fill in the cracks” left by triggered muons
- Improve overall sensitivity by 7%!



# Three-jet events

- Can recover another ~20% of signal from three-jet events
- Three-jet events have large  $t\bar{t}$  background — much more difficult to separate signal from background
- Sensitivity improvement of ~3%



# Acceptance improvement

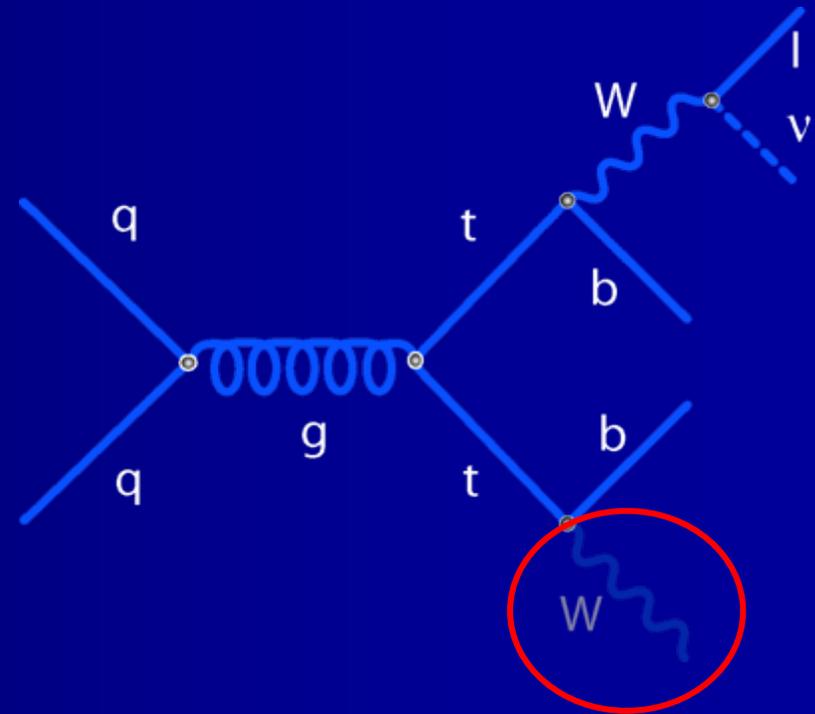
- Acceptance increases gives us more signal
- Luminosity scaling would give 88 expected events
- Now 125 single top events expected – 40% gain in signal acceptance!

CDF Run II Preliminary  
Predicted event yield with 2.2 fb<sup>-1</sup>

Process	2 jets	3 jets
s-channel	41.2 ± 5.9	13.5 ± 1.9
t-channel	62.1 ± 9.1	18.3 ± 2.7
Single top	103.3 ± 15.0	21.8 ± 4.6
tt	146.0 ± 20.9	338.7 ± 48.2
Diboson	63.2 ± 6.3	21.5 ± 2.2
Z + jets	26.7 ± 3.9	11.0 ± 1.6
W + bottom	461.6 ± 139.1	141.1 ± 42.6
W + charm	395.0 ± 121.8	108.8 ± 33.5
W + light	339.8 ± 56.1	101.8 ± 16.9
Multijet	59.5 ± 23.8	21.3 ± 8.5
Total background	1491.8 ± 268.6	754.8 ± 91.3
Total prediction	1595.1 ± 269.0	776.6 ± 91.4
Observed	1535	712

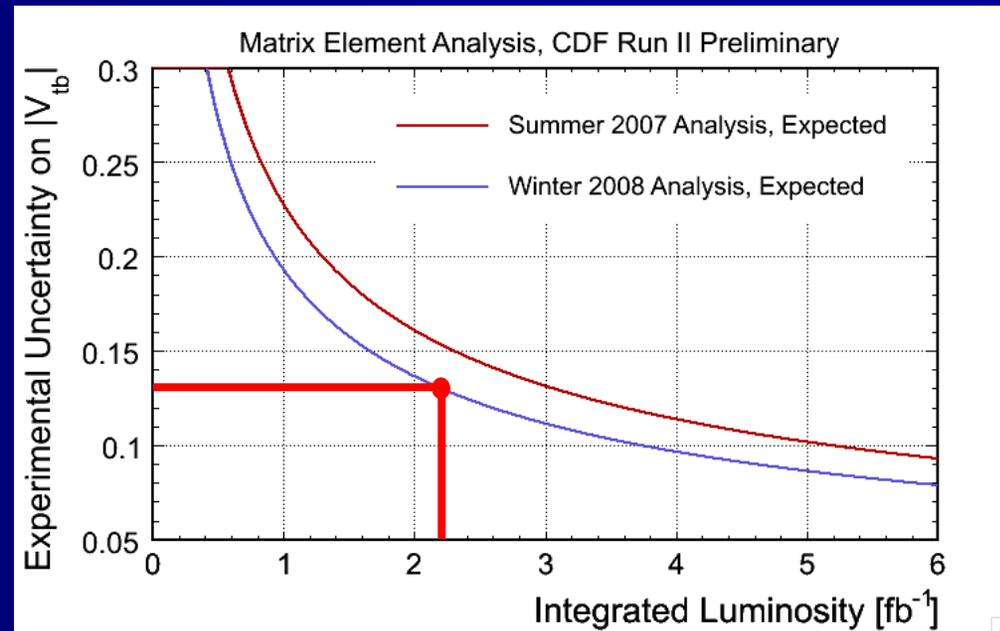
# $t\bar{t}$ matrix element

- Added  $t\bar{t}$  matrix element to matrix element method
- Assume a final-state  $W$  that has been missed (whether it decays leptonically or hadronically)
- Integrate over the unmeasured  $W$  particle to extract  $t\bar{t}$  probability
- Improves sensitivity by about 10%!

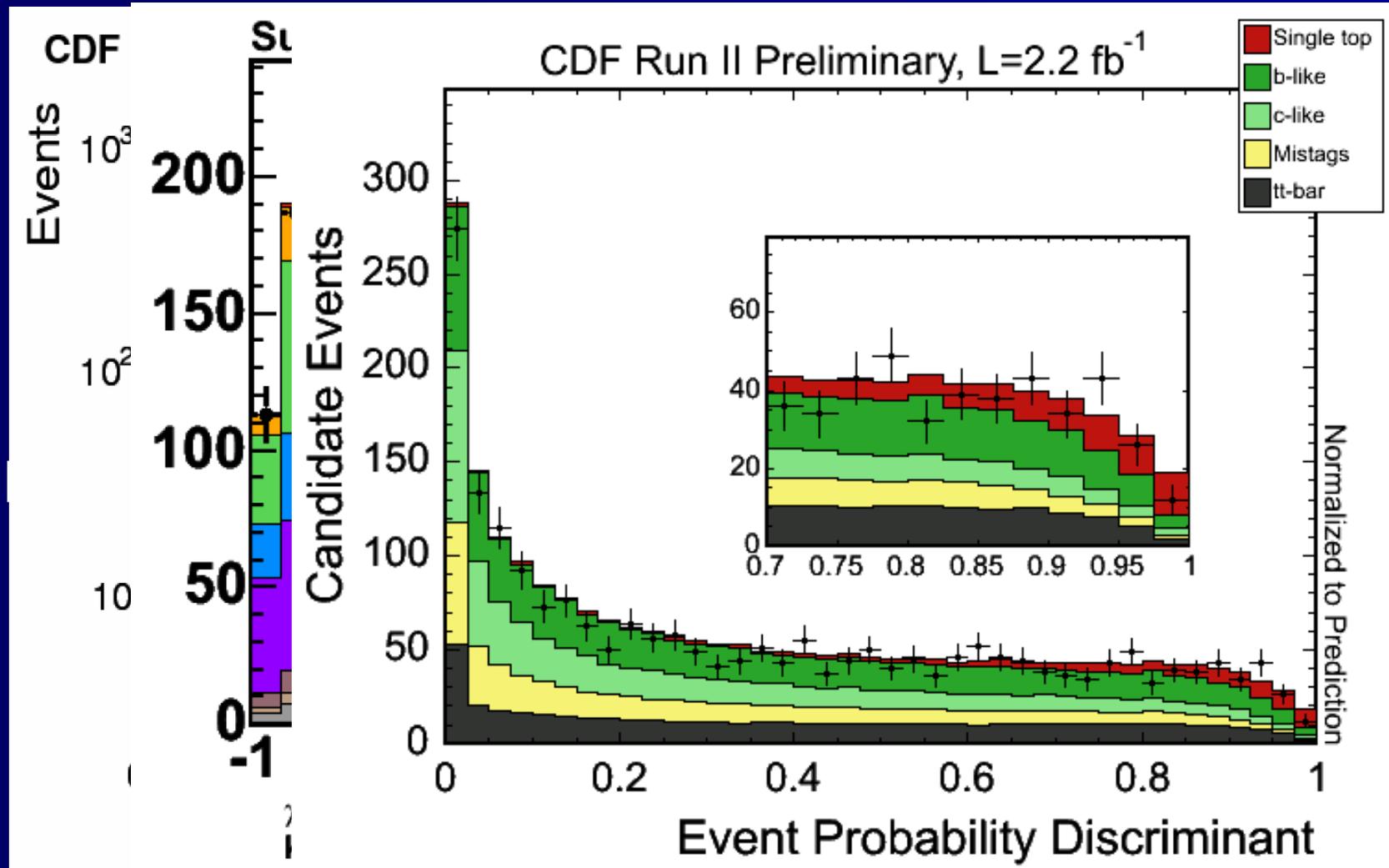


# Sensitivity improvement

- Several small improvements add up
- Expected uncertainty on  $|V_{tb}|$  for matrix element analysis increases by **~12%** compared to simple luminosity scaling
- Equivalent to a **56%** increase in data!



# CDF results

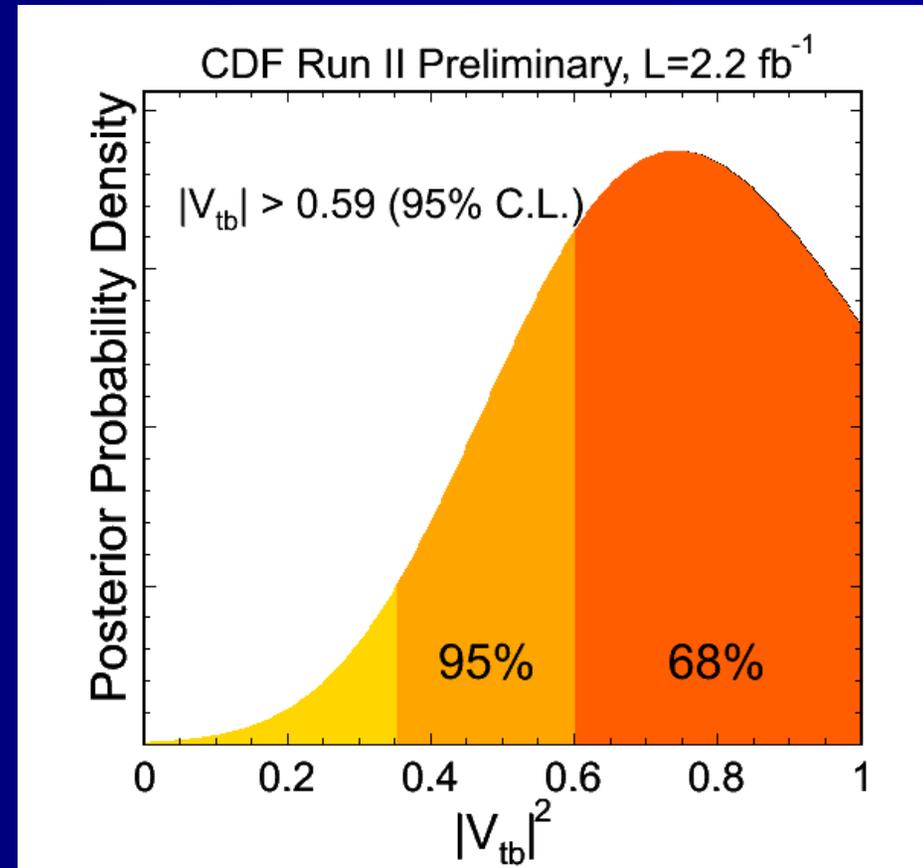


# CDF measurement of $|V_{tb}|$

## ■ Assume:

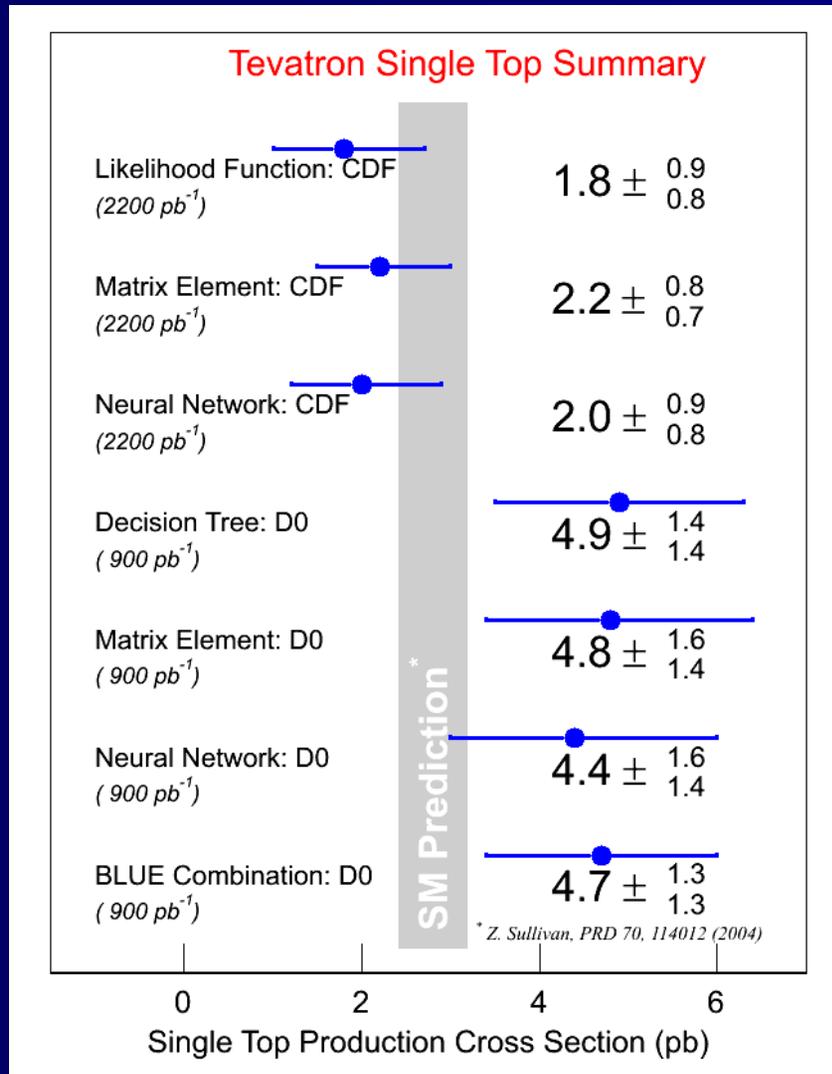
- Flat prior in  $|V_{tb}|^2$
- $0 < |V_{tb}|^2 \leq 1$
- $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$

## ■ Combined measurement and limit in preparation



$$|V_{tb}| = 0.88_{-0.12}^{+0.14} \text{ (experiment)} \pm 0.07 \text{ (theory)}$$

# Tevatron summary



- CDF combination in preparation

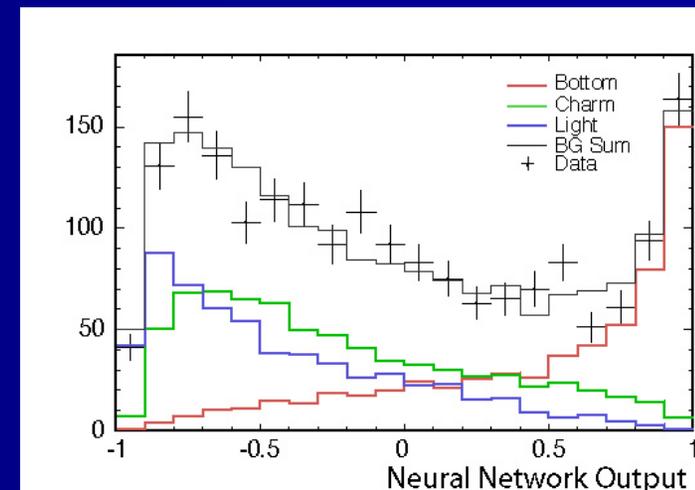
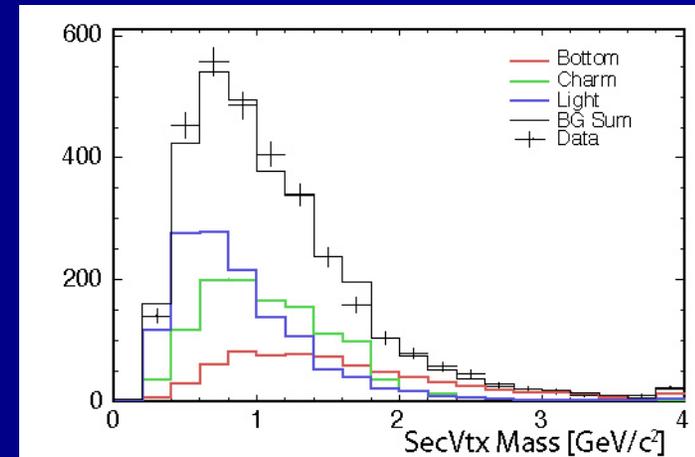
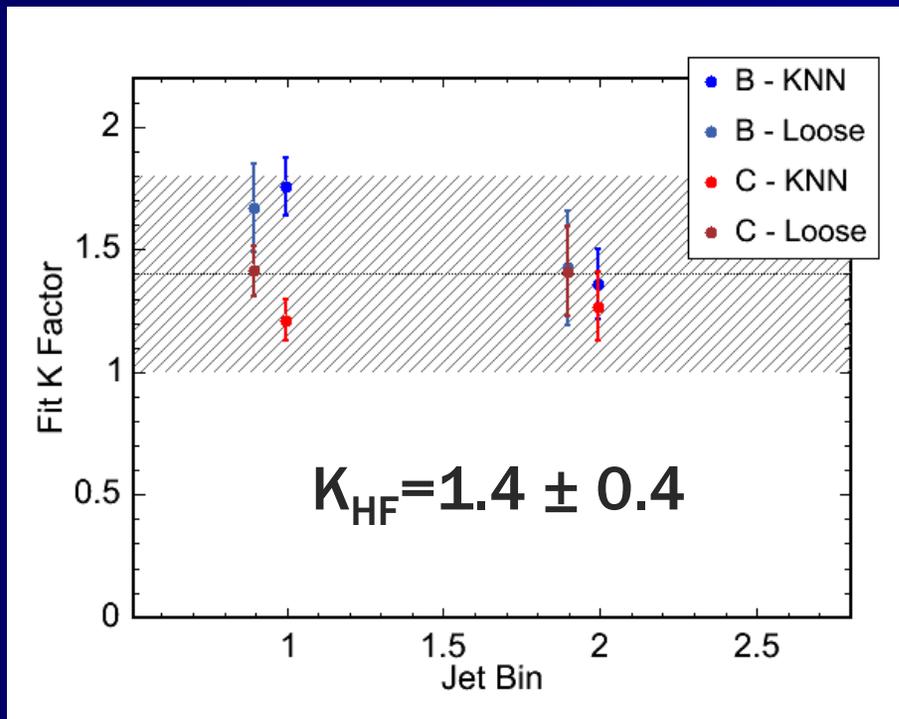
# Conclusion

- Measuring the single top cross section is very challenging!
- Multivariate analysis techniques are essential to increase sensitivity
- Both CDF and D0 have seen evidence of single top quark production
- We are able to directly measure  $|V_{tb}|$
- Now we enter the next stage:
  - Evidence for s- and t-channel production separately
  - Top quark polarization measurement
  - And, of course, onward to the Higgs!

**Backup slides**

# Heavy flavor calibration

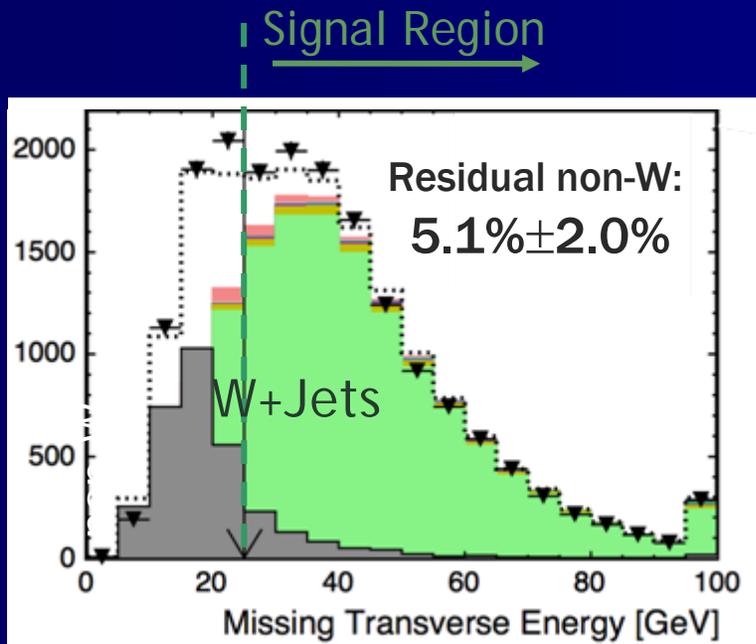
- Calibrate  $W +$  heavy flavor in  $W + 1$  jet data
- Three-parameter fit to bottom/charm/light templates of jet-flavor-separating distributions
- Correct for EWK/Top contributions
- Cross-check light flavor yield with prediction from mistag matrix



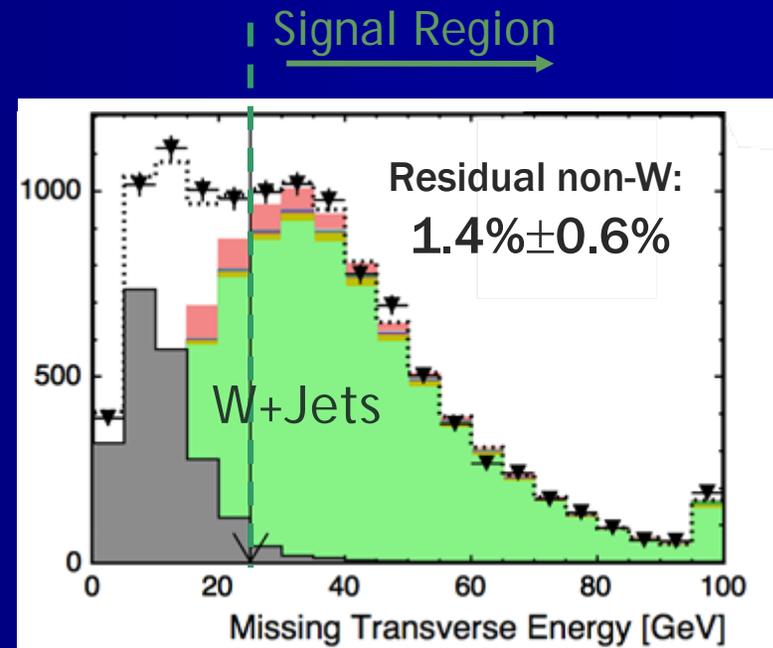
# Non-W background

- Build non-W model from data
- Invert non-kinematic lepton identification cuts
- Data is superposition of non-W and W+jets contribution
- Do likelihood fit to data

Electrons + 2 Jets

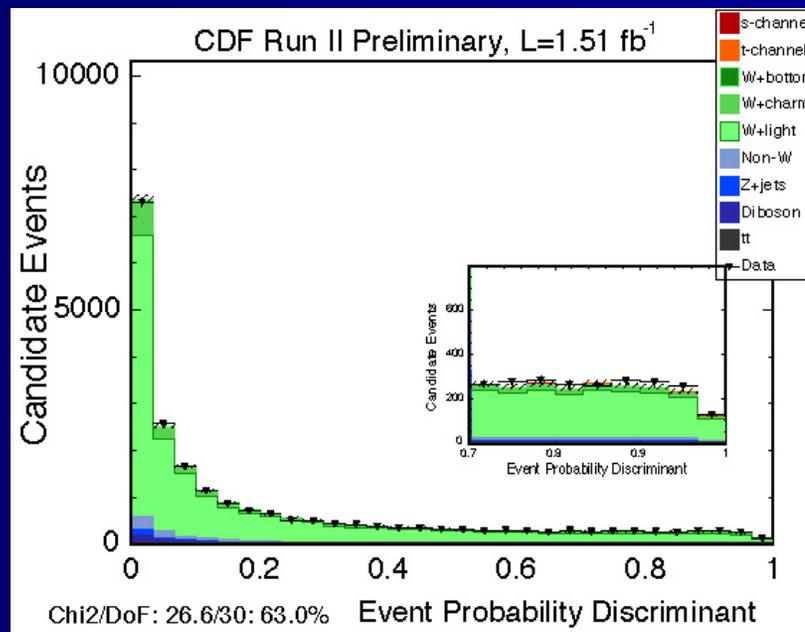


Muons + 2 Jets



# Matrix element cross-check

- Check the discriminant in the orthogonal untagged region to show that we model the data well
- Region is dominated by light jets — validates our modeling of  $W$  + jet kinematics



# Matrix element method

- Similar approach for both experiments
- CDF also includes jet flavor separator in discriminant to reduce contamination from light flavor jets:

$$EPD = \frac{b \cdot P_{Single\ top}}{b \cdot P_{Single\ top} + b \cdot P_{Wbb} + (1-b) \cdot P_{W+charm}}$$

# Systematic errors

## CDF Run II Preliminary

Systematic uncertainty	Range of Effect	Shape variations
Jet energy scale	0...16%	✓
Initial state radiation	0...11%	✓
Final state radiation	0...15%	✓
Parton distribution functions	2...3%	✓
Monte Carlo generator	1...5%	
Event detection efficiency	0...9%	
Luminosity	6%	
Neural net jet flavor separator		✓
Mistag model		✓
Non-W model		✓
Q <sup>2</sup> scale in Alpgen Monte Carlo		✓
Monte Carlo mismodeling		✓